

1) A trunnion mount hydraulic cylinder actuates the arm of a skid steer loader as shown below.

Write a geometric equation to determine lift angle θ when given cylinder/rod length e .

$$e^2 = (AB)^2 + (AC)^2 - 2(AB)(AC) \cos \theta$$

Compute lift angle θ for $e = 40$ inches. θ 61.131°

Write a geometric equation to determine lift speed $\dot{\theta}$ when given cylinder rod velocity \dot{e} .

$$e\dot{e} = (AB)(AC)\dot{\theta} \sin \theta \quad \dot{e} = -12 \text{ ips}$$

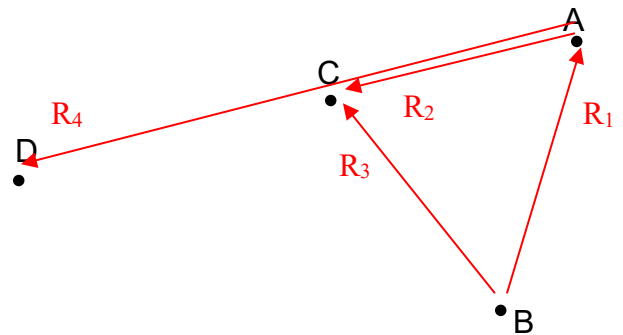
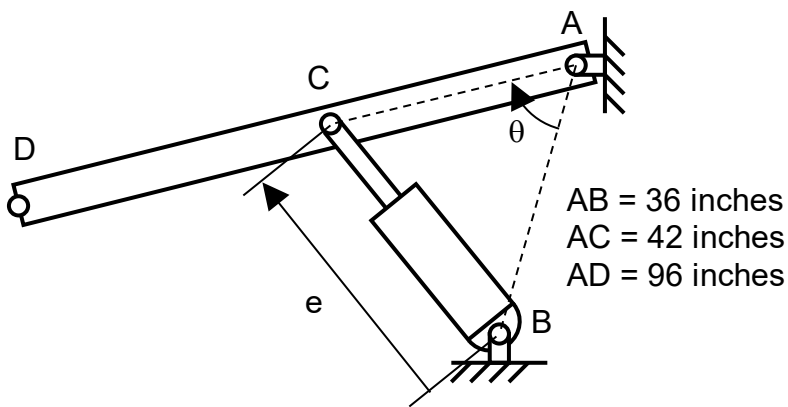
Compute lift speed $\dot{\theta}$ when the cylinder rod is retracting at 12 inches per second at this position.

$$\dot{\theta} \text{ -0.3625 rad/s = -20.77 deg/s}$$

Use the dots to the right of the picture to draw and label complex number vectors that model this mechanism. Write a position loop equation to analyze this mechanism.

$$\bar{R}_1 + \bar{R}_2 - \bar{R}_3 = 0$$

For each vector in your loop equation, complete the table describing if the length and angle of each vector are constant, variable, constrained or driver information.



Vector #	Length	Angle
1	constant	constant
2	constant	variable
3	driver	variable
4	constant	constrained

2) Program the two variable Newton-Raphson algorithm for position analysis of a four bar mechanism as shown in Notes_03_02 and Notes_03_03. Complete the table shown below. Provide hardcopy of your code.

Given: $r_1 = 90 \text{ cm}$, $r_2 = 30 \text{ cm}$, $r_3 = 60 \text{ cm}$, $r_4 = 45 \text{ cm}$, $\theta_1 = 0^\circ$, $\theta_2 = 10^\circ$

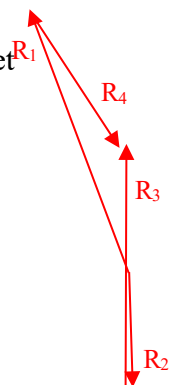
k	$\{q\} = \begin{Bmatrix} \theta_3 \\ \theta_4 \end{Bmatrix}$ [deg]	$\{\Phi\} = \begin{Bmatrix} f_H \\ f_V \end{Bmatrix}$ [cm]	$[\partial\Phi/\partial q]$ [cm/rad]	$[\partial\Phi/\partial q]^{-1}\{\Phi\}$ [rad]	$[\partial\Phi/\partial q]^{-1}\{\Phi\}$ [deg]
1	0 90	-0.4558 -39.7906	0 45.0000 60.0000 -0.0000	-0.6632 -0.0101	-37.9972 -0.5803
2	37.9972 90.5803	-12.7175 -2.8509	-36.9374 44.9977 47.2825 0.4558	-0.0571 -0.3295	-3.2727 -18.8797
3	41.2698 109.4600	-0.3674 2.3565	-39.5764 42.4293 45.0967 14.9917	0.0421 0.0306	2.4112 1.7530
4	38.8587 107.7071	-0.0472 -0.0146	-37.6441 42.8681 46.7218 13.6868	0.0000 -0.0011	0.0005 -0.0627
5	38.8581 107.7697	-0.00000820 0.00002564	$\det[\Phi_q]=$ -2519.2		

Check your solution by another method. Show your work. θ_3 38.86° θ_4 107.77°
checked using "Notes_03_01_four_bar_angles.xls"

3) Use your Newton-Raphson code to find θ_3 and θ_4 for the four bar portion of the sewing machine on page 5 of Notes_03_04 when the crank is straight down. Do not analyze the offset slider crank portion.

Given: $r_1 = 4.07 \text{ cm}$, $r_2 = 1.60 \text{ cm}$, $r_3 = 3.57 \text{ cm}$, $r_4 = 2.24 \text{ cm}$, $\theta_1 = 110.4^\circ$, $\theta_2 = 270^\circ$

θ_3 92.45° θ_4 304.41°



EXTRA CREDIT

Modify your Newton-Raphson algorithm to find θ_2 and θ_4 when $\theta_3 = 0^\circ$ for the four bar in part 2) above. Provide hardcopy of your code.

θ_2 97.18° θ_4 138.59° checked using "Notes_03_01_four_bar_angles.xls"

```
% h04_02_03.m - ME 481 H04 Newton-Raphson for four bar
% parts 2) and 3)
% HJSIII, 15.02.04

clear

% constants
d2r = pi /180;

% lengths and angles
r      = [ 90 30 60 45 ]; % [cm] - part 2
th_deg = [ 0 10 0 90 ]; % [deg] - part 2

r      = [ 4.07 1.60 3.57 2.24 ]; % [cm] - part 3
th_deg = [ 110.4 135 60 0 ]; % [deg] - part 3 posture in drawing
th_deg = [ 110.4 270 90 330 ]; % [deg] - part 3 crank straight down

th = th_deg * d2r;

% iteration loop
q = [ th(3) th(4) ]';
for iter = 1 : 5,
    th(3) = q(1);
    th(4) = q(2);
    iter
    q_deg = q / d2r

    PHI = [ r(2)*cos(th(2))+r(3)*cos(th(3))-r(4)*cos(th(4))-r(1)*cos(th(1)) ;
            r(2)*sin(th(2))+r(3)*sin(th(3))-r(4)*sin(th(4))-r(1)*sin(th(1)) ]

    JAC = [ -r(3)*sin(th(3))  r(4)*sin(th(4)) ;
            r(3)*cos(th(3))  -r(4)*cos(th(4)) ]

    update = inv(JAC) * PHI

    update_deg = update / d2r

    q = q - update;
    pause
end

det_JAC = det(JAC)

% bottom of h04_02_03
```

```
% h04_ec.m - ME 481 H04 Newton-Raphson for four bar
% extra credit
% HJSIII, 15.02.04

clear

% constants
d2r = pi /180;

% lengths and angles
r = [ 90 30 60 45 ]; % [cm]
th_deg = [ 0 97 0 138 ]; % [deg]
th = th_deg * d2r;

% iteration loop
q = [ th(2) th(4) ]';
for iter = 1 : 5,
    th(2) = q(1);
    th(4) = q(2);
    iter
    q_deg = q / d2r

    PHI = [ r(2)*cos(th(2))+r(3)*cos(th(3))-r(4)*cos(th(4))-r(1)*cos(th(1)) ;
            r(2)*sin(th(2))+r(3)*sin(th(3))-r(4)*sin(th(4))-r(1)*sin(th(1)) ]

    JAC = [ -r(2)*sin(th(2))    r(4)*sin(th(4)) ;
            r(2)*cos(th(2))    -r(4)*cos(th(4)) ]

    update = inv(JAC) * PHI

    update_deg = update / d2r

    q = q - update;
    pause
end

det_JAC = det(JAC)

% bottom of h04_ec
```