Name(s)

Homework 5

Due: In class, Friday, 9/28

1. (10 pts) For the system shown below, let l = 1.0 m, a = 0.45l, $k_t = 500$ N-m/rad and $k_1 = k_2 = 1000$ N/m. Also, the mass of the bar is m = 10 kg and gravity excluded.



- (1) (3 pts) The moment of inertia of the bar in kg-m² with respect to the pivot O is:
 - a) $J_o = 3.33$ b) $J_o = 3.97$ c) $J_o = 4.71$ d) $J_o = 5.82$ e) $J_o = 6.65$

(2) (7 pts) The natural frequency of the system in rad/s is:

- a) $\omega_n = 12.3$
- b) $\omega_n = 22.6$
- c) $\omega_n = 33.1$
- d) $\omega_n = 41.5$
- e) $\omega_n = 54.2$

2. (10pts) A ball of mass is attached to an elastic cord as shown below. The cord is stretched with a tension *T*. Assume the tension remains the same as the mass is pulled up by a small amount (ie. $\sin \theta = \tan \theta = \theta$). Furthermore, gravity is neglected.



- (1) (3 pts) The magnitude *and direction* of the vertical force, F_m , on the mass by the cord tension as a function of the displacement of the mass, x, is given by:
 - a) $F_m = -\left(\frac{Tl}{ab}\right) x$ b) $F_m = -\left(\frac{2Tl}{ab}\right) x$ c) $F_m = -\left(\frac{0.7Tl}{ab}\right) x$ d) $F_m = \left(\frac{Tl}{ab}\right) x$ e) $F_m = \left(\frac{2Tl}{ab}\right) x$ f) $F_m = \left(\frac{0.7Tl}{ab}\right) x$
- (2) (7 pts) Let l = 1.0 m, a = 0.7l, b = 0.3l, m = 0.1 kg and T = 100 N. If the ball is pulled up by an amount of $x_o = 1.0$ cm and then let go, the number of times the ball will bounce up and down in one second is equal to:
 - a) N = 11
 - b) *N* = 21
 - c) N = 31
 - d) N = 41
 - e) N = 51

3. (25 pts) A complex-shaped object of mass *m* is shown below. When it is suspended like a pendulum at point *A*, it swings 60 times in one minute.



- (1) (2pts) The natural frequency of the system in rad/s is
 - a) $\omega_n = \pi/2$ b) $\omega_n = \pi$
 - c) $\omega_n = 2\pi$ d) $\omega_n = 4\pi$
 - e) $\omega_n = 1.0$

(2) (4 pts) The governing equation for the pendulum in free swing motion is

- a) $J_A\ddot{\theta} + mgL\theta = 0$
- b) $L\ddot{\theta} + g\theta = 0$
- c) $2J_A\ddot{\theta} + mgL\theta = 0$
- d) $2L\ddot{\theta} + g\theta = 0$
- e) $J_A\ddot{\theta} + 2mgL\theta = 0$
- (3) (5 pts) Let m = 2.0 kg and L = 0.2 m. The moment of inertia of the object *about its center of mass* in kg-m² is about equal to
 - a) $J_{cg} = 0.009$
 - b) $J_{cg} = 0.019$
 - c) $J_{cg} = 0.038$
 - d) $J_{cg} = 0.076$
 - e) $J_{cg} = 0.098$

As worked out in class, the free vibration (ie. pendulum swing) is given by $\theta(t) = A\sin(\omega_n t + \phi)$. Suppose the pendulum is displaced by an angle of $\theta_o = 0.1$ rad and is released with a velocity of $\dot{\theta}_o = -0.5$ rad/s.

(4) (2pts) The amplitude of the pendulum swing in rad is about equal to

- a) A = 0.050
- b) A = 0.098
- c) A = 0.128
- d) A = 0.187
- e) A = 0.245
- (5) (2pts) The phase angle in rad of the pendulum swing is about equal to
 - a) $\phi = \pi / 4$
 - b) $\phi = 0.94$
 - c) $\phi = 2.24$
 - d) $\phi = -1.54$
 - e) $\phi = -2.76$
- (5) (10pts) Write a simple matlab program to calculate θ vs. *t* and plot the pendulum swing for two periods of pendulum swing. Make sure your plot shows a smooth curve. Also, make sure your plot matches the given ICs to be correct. Label your plot including units. Submit your matlab program along with results. (the class website has a simple matlab guide)