Name(s)

Homework 9

Due: In class, Friday Oct. 26

1. (32 pts) Examine the geometric model shown below, where y(t) is a motion input applied at the right end of damper c_1 . The math model for the system is $m\ddot{x} + (c_1 + c_2)\dot{x} + kx = c_1\omega Y sin(\omega t + \pi)$



(1) (4 pts) The magnitude of the follow-up vibration $x_p(t) = X \sin(wt + \pi + \psi)$ is

a)
$$X = \frac{c_1 r Y}{m \omega_n} \frac{1}{\left[(1 - r^2)^2 + (2\xi r)^2 \right]^{1/2}}$$

b)
$$X = \frac{Y / \omega_n^2}{\left[(1 - r^2)^2 + (2\xi r)^2 \right]^{1/2}}$$

c)
$$X = \frac{c_1 Y}{m \omega_n^2} \frac{1}{\left[(1 - r^2)^2 + (2\xi r)^2 \right]^{1/2}}$$

d)
$$X = \frac{r^2 Y}{\left[(1 - r^2)^2 + (2\xi r)^2 \right]^{1/2}}$$

(2) (8 pts) The magnitude of the force $f_Q(t) = F_Q \sin(wt + \alpha)$ on damper c_1 is a) $F_Q = \left[(1 - r^2)^2 + (2\xi r)^2 \right]^{1/2} X$ b) $F_Q = \left[(k - m\omega^2)^2 + (c_2\omega)^2 \right]^{1/2} X$ c) $F_Q = \left[(1 - r^2)^2 + (2\xi r)^2 \right]^{1/2} kX$ d) $F_Q = \left[(k - m\omega^2)^2 + (c_2\omega)^2 \right]^{1/2} c_1 X$

(hint: this force may be more easily obtained starting with the elemental equation of the mass).

(3) (5 pts) The magnitude of the force $f_P(t) = F_P \sin(wt + \beta)$ transmitted to the wall at point *P* is a) $F_P = [k^2 + (c_2 \omega)^2]^{1/2} X$ b) $F_P = [(k - m\omega^2)^2 + (c_2 \omega)^2]^{1/2} c_2 X$ c) $F_P = [(1 - r^2)^2 + (2\xi r)^2]^{1/2} kX$ d) $F_P = [(1 - r^2)^2 + (2\xi r)^2]^{1/2} X$

(4) (15 pts) Let m = 10 kg, k = 1000 N/m, $c_1 = 110$ N-s/m, and $c_2 = 25$ N-s/m. Program in matlab to plot X/Y vs. ω/ω_n and F_P/F_Q vs. ω/ω_n for r ranging from 0 to 2. Submit the matlab program and the plots. From the plots, use matlab data curser tool to determine the maximum values of X/Y and F_P/F_Q and the corresponding values of r:

 $\max(X/Y) = \underline{\qquad} corresponding \quad r = \underline{\qquad}$ $\max(F_P/F_0) = \underline{\qquad} corresponding \quad r = \underline{\qquad}$

2. (15 pts) A machine with a rotating unbalance, $m_o e$, is mounted on a rubber floor as shown. The total mass of the machine is $m_t = 120$ kg, the rubber-mount stiffness is $k = 8 \times 10^5$ N/m and damping constant c = 9000 N-s/m. The centrifugal force generated by the machine unbalance is determined to be $F_o = 600$ N when the machine operates at $\omega = 1500$ rpm.



(1) (2 pts) The machine unbalance in kg-m is

- a) $m_o e = 0.024$ b) $m_o e = 0.042$
- c) $m_o e = 0.064$ d) $m_o e = 0.092$
- (2) (4 pts) The magnitude of machine vibration in millimeter is
- a) X = 0.11 b) X = 0.23
- c) X = 0.45 d) X = 0.86

(3) (4 pts) The magnitude of the force in Newton transmitted to machine foundation is

- a) $F_{to} = 102$ b) $F_{to} = 243$
- c) $F_{to} = 377$ d) $F_{to} = 458$

(4) (5 pts) To reduce the transmitted force by 25%, the damping constant, c, in N-s/m of the rubber floor needs to be at least

- a) larger than 10410
- b) larger than 12540
- c) smaller than 4558
- b) smaller than 6758

3. (10 pts) A vehicle is traveling through a road segment of wavy pavement and develops an uncomfortable bouncing vibration of magnitude X = 0.1 m. The pavement may be described by a sine wave of amplitude Y = 0.1 m and wavelength $\lambda = 3.0$ m. The bouncing vibration of the vehicle may be meaningfully modeled by the SDOF model below



The governing equation was derived in class to be

$$m\ddot{x} + c\dot{x} + kx = Y\sqrt{k^2 + c^2\omega^2}\sin\omega t$$

Let m = 500 kg, c = 10000 N-s/m and $k = 2 \times 10^5$ N/m.

(1) (5 pts) The traveling speed of the vehicle in *mph* is

- a) v = 15
- b) v = 20
- c) v = 25
- d) v = 30

(2) (5 pts) To cut down the bounce to one quarter of the original value, the vehicle needs to at least travel

- a) faster than 45 mph
- b) faster than 90 mph
- c) slower than 10 mph
- d) slower than 12 mph