Today, we will:

- Review how to match a pump and a piping system.
- Do some example problems – matching pumps to systems
- Begin to discuss dimensionless parameters in pump performance

From previous lecture…the head form of the conservation of energy equation:

$$\frac{P_1}{\rho_1 g}+\alpha_1\frac{V_1^2}{2g}+z_1+h_{\text{pump,u}}=\frac{P_2}{\rho_2 g}+\alpha_2\frac{V_2^2}{2g}+z_2+h_L$$

Solve for H = net pump head delivered = $h_{\text{pump,u}}$ = useful pump head:

$$h_{\text{pump,u}}=\underbrace{\frac{P_2}{\rho_2 g}-\frac{P_1}{\rho_1 g}}_{\text{I}}+\underbrace{\frac{\alpha_2 V_2^2-\alpha_1 V_1^2}{2g}}_{\text{II}}+\underbrace{z_2-z_1}_{\text{III}}+\underbrace{h_L}_{\text{IV}} \qquad (1)$$

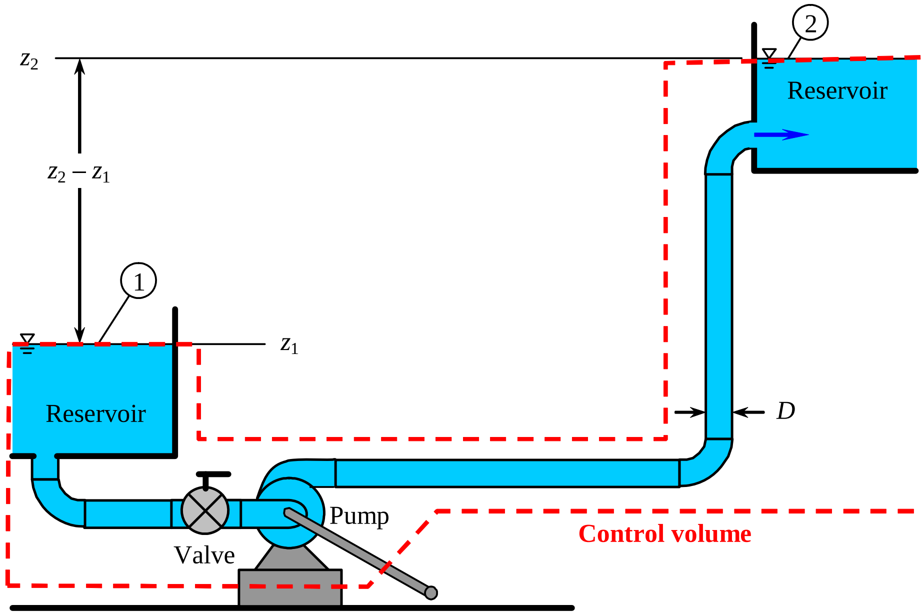
Consider a typical piping system with a pump that pumps water from a lower reservoir to a higher reservoir. In general, from Eq. (1), we see that the pump must do four things:

I Change the pressure in the flow from inlet to outlet

II Change the kinetic energy in the flow from inlet to outlet

III Change the elevation in the flow from inlet to outlet

IV Overcome irreversible head losses

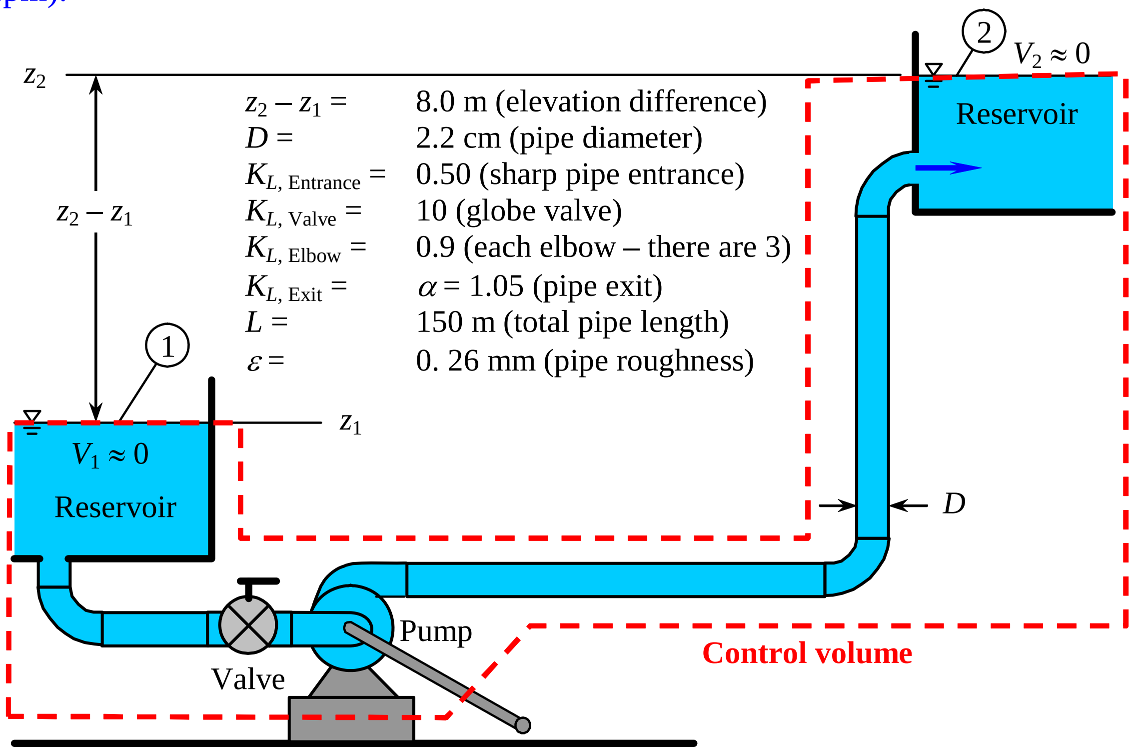


Example Problem – Matching a Pump to a Piping System

Given: Water (ρ = 1000 kg/m^3, μ = 1.00 × 10^{-3} kg/m·s) is pumped from one large reservoir to another large reservoir that is at a higher elevation. The free surfaces of both reservoirs are exposed to atmospheric pressure, as sketched. The dimensions and minor loss coefficients are provided in the figure. The pipe is 2.2 cm I.D. cast iron pipe. The total pipe length is 150.0 m. The entrance and exit are sharp. There are three regular threaded 90-degree elbows, and one fully open threaded globe valve. The pump's performance (supply curve) is approximated by the expression

$$H_{\text{available}} = h_{\text{pump, u supply}} = H_0 - a\dot{V}^2$$

where shutoff head H_0 = 20.0 m of water column, coefficient a = 0.072 m/Lpm^2, available pump head $H_{\text{available}}$ is in units of meters of water column, and volume flow rate $\dot{V}$ is in units of liters per minute (Lpm).



To do: Calculate the volume flow rate through this piping system.

Solution:

- First we draw a control volume, as shown by the dashed line. We cut through the pump shaft and through the surface of both reservoirs (inlet 1 and outlet 2), where we know that the velocity is nearly zero and the pressure is atmospheric. The rest of the control volume simply surrounds the piping system.
- We apply the head form of the energy equation from the inlet (1) to the outlet (2):

$P_1 = P_2 = P_{\text{atm}}$

$V_1 = V_2 \approx 0$

$$\frac{P_1}{\rho g} + \alpha_1 \frac{V_1^2}{2g} + z_1 + h_{\text{pump,u}} = \frac{P_2}{\rho g} + \alpha_2 \frac{V_2^2}{2g} + z_2 + h_{\text{turbine,e}} + h_L$$

We will call this $h_{\text{pump, u, system}}$ since it is the required pump head for the given piping system.

The rest of this problem will be solved in class.