M E 320	Professor John M. Cimbala	Lecture 24
Today, we will:		
1 .	p performance curves to match a pump and a piping system, and do some e	example problems
2. Pump Performa a. Pump perfor		
(<i>H</i> is the same	literature and terminology, <i>H</i> is the net head of the p as what we called $h_{pump,u}$ in the energy equation, i.e., ne pump to the fluid.) So, $h_{pump,u} = H$	- -
Also recall, pu	Imp efficiency is defined as	

n -	_ useful power delivered to the fluid	_ water horsepower	$\dot{mgh}_{pump,u}$	ρVġΗ
η _{pump} -	shaft power required to run the pump	brake horsepower	bhp	bhp

b. Matching a pump to a pumping system

General Example: Matching a pump to a system.

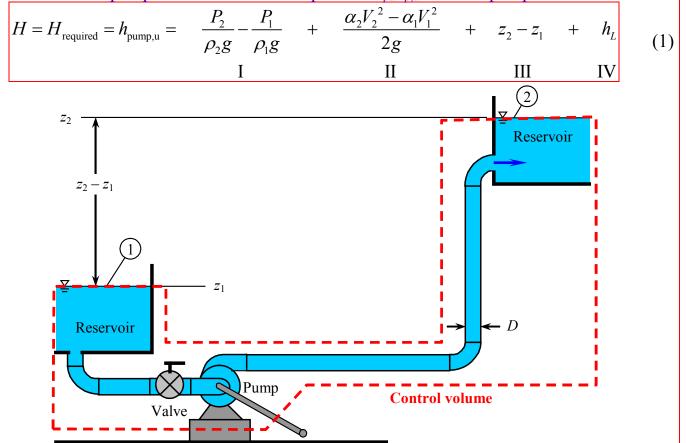
Given: Consider a typical piping system with a pump that pumps water from a lower reservoir to a higher reservoir. All diameters, heights, minor loss coefficients, etc. are known.

To do: Predict the volume flow rate.

Solution: As always we start by drawing a wise control volume. See CV as drawn. Then we apply the head form of the conservation of energy equation for a CV from 1 to 2:

$$\frac{P_1}{\rho_1 g} + \alpha_1 \frac{V_1^2}{2g} + z_1 + h_{\text{pump},u} = \frac{P_2}{\rho_2 g} + \alpha_2 \frac{V_2^2}{2g} + z_2 + h_{\text{turbine},e} + h_L$$
No turbine here

Solve for H = net pump head delivered or required = $h_{pump,u}$ = useful pump head:



In general, from Eq. (1), we see that the pump must do four things:

I Change the pressure in the flow from inlet to outlet

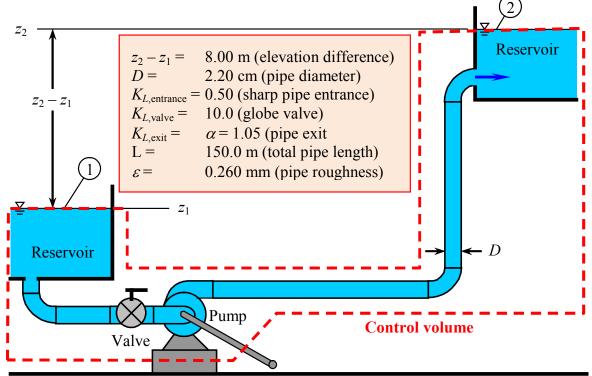
- II Change the kinetic energy in the flow from inlet to outlet
- III Change the elevation in the flow from inlet to outlet
- IV Overcome irreversible head losses

Example: Matching a Pump to a Piping System

Given: Water ($\rho = 1000 \text{ kg/m}^3$, $\mu = 1.00 \times 10^{-3} \text{ kg/m} \cdot \text{s}$) is pumped from one large reservoir to another large reservoir that is at a higher elevation. The free surfaces of both reservoirs are exposed to atmospheric pressure, as sketched. The dimensions and minor loss coefficients are provided in the figure. The pipe is 2.20 cm I.D. cast iron pipe. The total pipe length is 150.0 m. The entrance and exit are sharp. There are three regular threaded 90-degree elbows, and one fully open threaded globe valve. The pump's performance (supply curve) is approximated by the expression

$$H_{\text{available}} = h_{\text{pump,u, supply}} = H_0 - a V^2$$

where shutoff head $H_0 = 20.0$ m of water column, coefficient a = 0.0720 m/Lpm² = 2.592×10^8 s²/m², available pump head $H_{\text{available}}$ is in units of meters of water column, and volume flow rate \dot{V} is in units of liters per minute (Lpm).



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To do: Calculate the volume flow rate through this piping system.

Solution:

- First we draw a control volume, as shown by the dashed line. We cut through the pump shaft and through the surface of both reservoirs (inlet 1 and outlet 2), where we know that the velocity is nearly zero and the pressure is atmospheric. The rest of the control volume simply surrounds the piping system.
- We apply the head form of the energy equation from the inlet (1) to the outlet (2):

$$\frac{P_1 = P_2 = P_{atm}}{\frac{P_1}{\sqrt{2}g} + \alpha_1 \frac{V_2^2}{\sqrt{2}g} + z_1 + h_{pump,u}}{\frac{P_2}{\sqrt{2}g} + \alpha_2 \frac{V_2^2}{\sqrt{2}g} + z_2 + h_{turbing}} + h_L$$

The rest of this problem will be solved in class.
We call this $h_{pump, u, system} = H_{required}$ since it is the required pump head for the given piping system.

e is exactly what I typed into the main "Equations Window" of EES:	Đ	
'EES Solution for the class example problem - matching a pump to a pi		
'Constants:" Deltaz = 8.0 [m] ho = 1000 [kg/m^3] mu = 1.00e-3 [kg/(m*s)] D = 0.022 [m]		
L = 150 [m] SigmaK_L = 0.5 + 10 + 3*0.9 + 1.05 epsilon = 0.00026 [m] g = g# "(gravitational constant, predifined by EES)"		
'Pump performance curve:" H_0 = 20.0 [m] a_pump = 2.592e8 [s^2/m^5]		
'Equations:" Re = (rho*D*V)/mu v_dot = V*PI*(D^2)/4 n_pump_u_supply = H_0 - a_pump*V_dot^2 n_pump_u_system = 8*V_dot^2/(PI^2*g*D^4)*(f*L/D + SigmaK_L) + De n_pump_u_supply = h_pump_u_system v_dot_LPM = V_dot*Convert(m^3/s,L/min)	eltaz	
	k equation"	

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h_pump_u_system	1.00000	-infinity		N 6								
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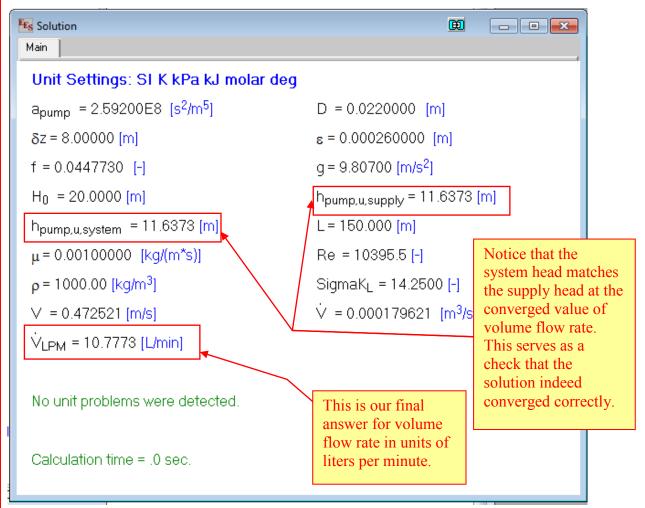
Here is what the <u>Windows-Formatted Equations</u> window looks like (much "cleaner" looking equations – and easier to spot typo errors):

EES Solution for the class example problem - matching a pump to a piping system, J. M. Cimbala Constants: δz = 8 [m] $\rho = 1000 \, [kg/m^3]$ $\mu = 0.001 [kg/(m*s)]$ D = 0.022 [m] L = 150 [m] $SigmaK_L = 0.5 + 10 + 3 \cdot 0.9 + 1.05$ $\epsilon = 0.00026$ [m] $g = 9.807 [m/s^2]$ (gravitational constant, predifined by EES) Pump performance curve: $H_0 = 20$ [m] $a_{pump} = 2.592 \times 10^8 [s^2/m^5]$ Equations: $Re = \frac{\rho \cdot D \cdot V}{\mu}$ $\dot{\mathbf{V}} = \mathbf{V} \cdot \pi \cdot \frac{\mathbf{D}^2}{4}$ $h_{pump,u,supply} = H_0 - a_{pump} \cdot \dot{V}^2$ $h_{pump,u,system} = 8 \cdot \frac{\dot{V}^2}{\pi^2 \cdot g \cdot D^4} \cdot \left[f \cdot \frac{L}{D} + SigmaK_L\right] + \delta z$ $h_{pump,u,supply} = h_{pump,u,system}$ $\dot{\mathbf{V}}_{\text{LPM}} = \dot{\mathbf{V}} \cdot \left[60000 \cdot \frac{\text{L/min}}{\text{m}^{3}/\text{c}} \right]$

$$\frac{1}{\sqrt{f}} = -2 \cdot \log \left[\frac{\epsilon}{D \cdot 3.7} + \frac{2.51}{\text{Re} \cdot \sqrt{f}} \right]$$
 Colebrook equation

To solve, click on Calculate and then Solve. Note that it does not converge unless you change the limits and guesses in Options-Variable Info

Finally, <u>Calculate</u> and <u>Solve</u> (or click on the calculator icon) to yield the solution, as shown in the Solution window:



Note: It is also possible to plot with EES. Here is a plot of supply head and system head as functions of volume flow rate. As you can see, they intersect at the operating point, which is around 10.8 Lpm.

