

M E 345 - Instrumentation, Measurements, and Statistics

Today, we will:

- Introduce the course and instructor: **John M. Cimbala**, 863-2739, jmc6@psu.edu
- Briefly go over the course website at www.mne.psu.edu/me345
- Review first pdf module: **Introduction to Mechanical Engineering Measurements**
- Do some practice questions and example problems
- If time, show some hints about plotting in Excel.

Practice Questions:

1. How many significant digits are in each of these numbers?

(no decimal point if integer)

Number	Number of sig. digits	Exponential notation
603.	3	6.03×10^2
600	∞ (integer)	6×10^2 or 600×10^0
<u>6</u> 00	2	6.0×10^2
0.007	1	7×10^{-3}
1.005	4	1.005×10^0
<u>7</u>	∞ (integer)	7×10^0
7.	1	7×10^0
50.	2	5.0×10^1
0.01070	4	1.070×10^{-2}
732,000	∞ (integer)	732×10^3
732, <u>0</u> 00	5	7.3200×10^3
732, <u>0</u> 00	3	7.32×10^3
732,000.	6	7.32000×10^3

2. What is $2.00/3.0$?

$\downarrow$ 2 sig. digits
 $\downarrow$ 3 sig. digits
 Our answer is limited to 2 sig. digits for multiplication / division

Ans = 0.66666... But must round to 2 digits

★ **ANSWER = 0.67**

NOTE: • Do not use 0.67 for any subsequent calculations, since it is rounded

• To avoid round-off error, use more digits for further calculations, e.g., use 0.666667

Example: Significant digits

Given: 3 measurements with 3 different instruments

- i) 134,290 (5 significant digits)
- ii) 0.2875 (4 significant digits)
- iii) 29.473 (5 significant digits)

(a) To do: Round each number to 3 significant digits.

Solution:

- i) $134,000$ or 1.34×10^5
- ii) 0.288 (following convention, round up since 7 is odd)
- iii) 29.5

(b) To do: Add the 3 numbers and report the answer to the appropriate number of significant digits.

- i) 134,290 (5 significant digits)
- ii) 0.2875 (4 significant digits)
- iii) 29.473 (5 significant digits)

Solution:

- Align the decimal places
- Add
- Answer reported to left-most least significant digit

$$\begin{array}{r} 134,290. \\ 0.2875 \\ 29.473 \\ \hline 134,319.7605 \end{array}$$

Answer: $134,320$ or 1.3432×10^5

(c) To do: Multiply the first two numbers and report the answer to the appropriate number of significant digits.

- i) 134,290 (5 significant digits)
- ii) 0.2875 (4 significant digits)
- iii) 29.473 (5 significant digits)

Solution:

Answer: 38610

$$134,290 \times 0.2875 = 38608.375$$

5 digits 4 digits

Answer must be limited to 4 sig. dig.

Notes:

- Again, do not use this for any further calculations to avoid round-off error. Instead, use 38608.375
- Other answers, like 38608.4, are okay since you clearly indicate 4 sig. digits in your answer.

Example: Significant digits – Gas mileage calculations

(a) **Given:** You travel 210.0 miles in your new car, and use 7.00 gallons of gas.

To do: Calculate your gas mileage in units of miles per gallon. Give your answer to the appropriate number of significant digits.

Solution:

$$\text{mpg} = \frac{210.0 \text{ mi}}{7.00 \text{ gal}} = 30.0000 \text{ mpg}$$

4 sig. digits (above 210.0)
3 sig. digits (below 7.00)

But, answer is limited to 3 significant digits

$$\text{Answer} = \boxed{30.0 \text{ mpg}}$$

(more properly, write 28.)

(b) **Given:** You estimate that your car gets 28 miles per gallon. Gas costs \$3.899 per gallon.

To do: How much does it cost to travel 455 miles? Give your answer to the appropriate number of significant digits.

Solution:

Note: Need to create an equation based on the units

$$\text{Cost} = \frac{(455 \text{ miles}) \left(\frac{\$3.899}{\text{gal}} \right)}{28. \frac{\text{miles}}{\text{gal}}} = \$63.3588$$

But, 28. is only 2 sig. digits (it is not an integer).

So, Answer should be given to 2 sig. digits also.

$$\text{Answer} = \boxed{\$63.} \text{ or } \boxed{\$63} \text{ } [\$63.4 \text{ also ok}]$$

(c) **Given:** You fill up your tank, drive 316.5 miles, and pay \$44.89 to fill up your tank again. Gas costs \$3.799 per gallon. [Assume we fill the tank to exactly the same level.]

To do: Calculate your gas mileage in units of miles per gallon. Give your answer to the appropriate number of significant digits.

Solution:

• Again, use units to create the equation

$$\text{mpg} = \frac{(316.5 \text{ miles}) (\$3.799/\text{gal})}{\$44.89}$$
$$= 26.78511 \text{ mpg}$$

• But limit final answer to 4 digits

$$\text{Answer} = \boxed{26.79 \text{ mpg}}$$

Example: Significant digits – pressure

Given:

- Atmospheric pressure $P_{\text{atm}} = 101.3 \text{ kPa}$
- Gage pressure at point 1 is $1,350 \text{ Pa}$
- Gage pressure is defined as $P_{\text{gage}} = P - P_{\text{atm}}$, where P = absolute pressure

To do: Calculate the absolute pressure at location 1, taking into account the appropriate number of significant digits.

Solution:

$$P_{\text{gage},1} = P_1 - P_{\text{atm}} \rightarrow P_1 = P_{\text{atm}} + P_{\text{gage}}$$

$$\begin{array}{r} P_1 = 101.\underline{3} \text{ kPa} \\ + 1.\underline{350} \text{ kPa} \\ \hline 102.\underline{650} \text{ kPa} \end{array}$$

← Align decimal pts

Converted to kPa so
we can add !!

★

Finally, limit answer to the left-most least significant digit

Ans. $P_1 = 102.6 \text{ kPa}$

Note: Use $P_1 = 102.65 \text{ kPa}$ for all subsequent calculations
to avoid round-off error