

Today, we will:

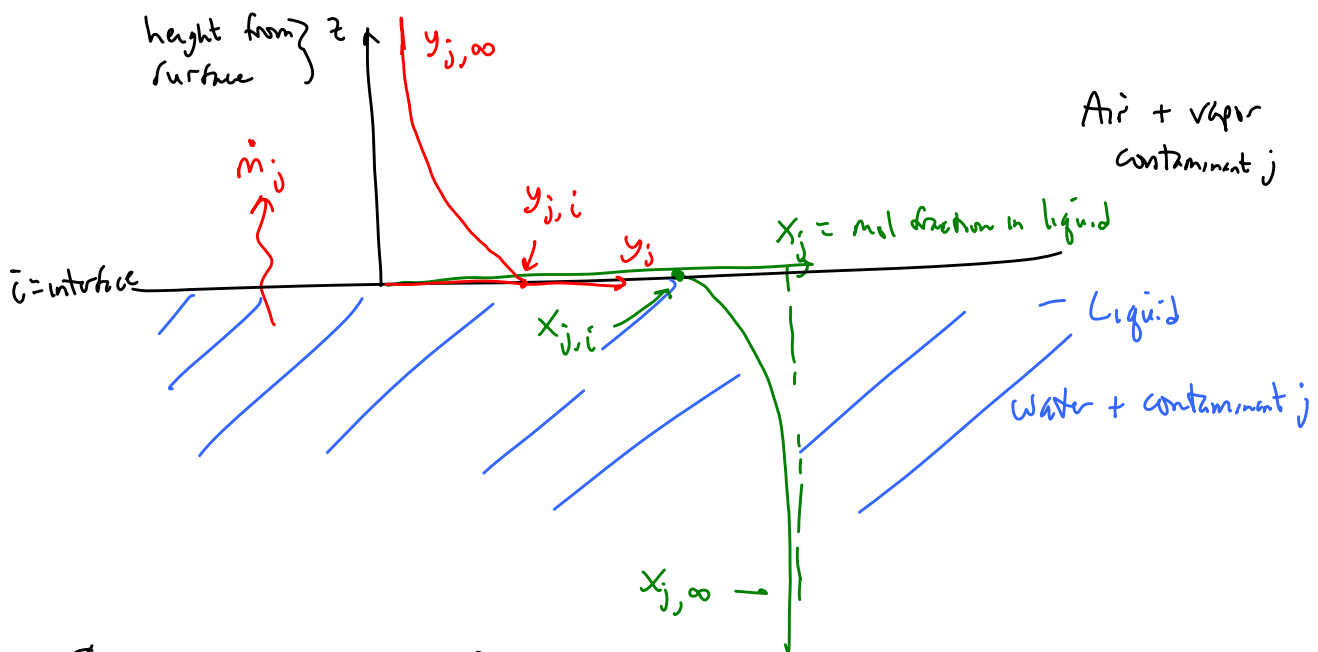
- Begin **Chapter 4 – Emission Rates**
- Discuss some definitions and notation
- Discuss **Emission Factors** in **Section 4.3**
- Do some example problems
- Discuss **Flux Chambers** in **Section 4.1**
- Do some example problems

2 s's, one m (know how to spell emission  
i, emitted)

• Goal – to predict how much pollution is being emitted by a source

• Definitions & notation:

Subscripts:  $j$  = species eg.  $y_j$  = mol fraction of species  $j$   
 $i$  = interface (between a liquid & air + vapor)



$\dot{S}_j$  = source strength of species  $j$   
 $\dot{m}_j$  = emission rate of species  $j$  } same thing.  $\boxed{\dot{m}_j = \dot{S}_j}$   
 = generation rate

Recall, in a duct, or a stack (chimney)  $\boxed{\dot{m}_j = C_j Q} = C_j \dot{V}$

•  $\dot{S}_j$  (lower case) =  $\frac{\dot{S}_j}{A}$  = source strength per unit area

$$\{\dot{m}_j\} = \{S_j\} = \left\{ \frac{m_{\text{all}}}{\text{time}} \right\}$$

$$\{S_j\} = \left\{ \frac{m_{\text{all}}}{\text{time} \cdot \text{area}} \right\}$$

★ Define  $\text{EF} = \text{Emission factor} \equiv \frac{\text{mass of contaminant emitted}}{\text{mass of raw material used}}$  ★

EPA publishes EF's for various processes

See App. A-2 through A-7, also see EPA's website

EF's are "quick & dirty" estimator for emission rate calculations

EPA document for EF's is called AP-42

"AP-42 Emission Factor"

NOTE: ALL THE EF's are for uncontrolled processes  
(no air pollution control system) (APCS) to cut down the emission

If an APCS is used, define  $\eta \equiv \text{removal efficiency}$

(eg.  $\eta = 90\%$  means that 90% of the pollutant is removed before discharging to the atmosphere)

★  $\dot{m}_d = (1 - \eta) \dot{m}_g$

discharged (under  $\dot{m}_d$ )      generates (under  $\dot{m}_g$ )

EF, correspond to  $\dot{m}_g$ , not  $\dot{m}_d$

[EF has many different units]

EF's are "ballpark" estimator — typically good to only 1 or at most 2 significant digits.

### Example

**Given:** A steel mill has an open hearth furnace with which it does melting and refining. The furnace refines about 8 tons of steel per hour on average.

**To do:** Estimate the uncontrolled emission rate of particles in kg/hr.

**Solution:**

See App A.2 (p. 781) open hearth furnace  $\rightarrow$   $EF = 10.55 \frac{\text{kg particles}}{\text{Mg steel}}$

Comments •  $M_g = 10^6 \text{ g}$

• EPA should know better than to list EF to 4 sig. digits!

$$\begin{aligned} \dot{m}_{\text{particles}} &= 8 \frac{\cancel{\text{ton steel}}}{\text{hr}} \times \frac{10.55 \text{ kg part}}{\cancel{\text{Mg steel}}} \left( \frac{2000 \cancel{\text{lbm steel}}}{\cancel{\text{ton steel}}} \right) \left( \frac{1 \cancel{\text{kg steel}}}{2.205 \cancel{\text{lbm steel}}} \right) \times \\ &\quad \times \left( \frac{1 \cancel{\text{Mg steel}}}{1000 \cancel{\text{kg steel}}} \right) = 76.5 \frac{\text{kg part.}}{\text{hr}} \end{aligned}$$

$$\dot{m}_{\text{particles}} \approx 80 \frac{\text{kg}}{\text{hr}}$$

### Example

**Given:** A small kerosene space heater is used for supplemental heating of a home. It burns 1 gallon of kerosene in about 5 hours.

**To do:** Estimate the uncontrolled emission rate of carbon monoxide into the room in units of g/hr.

**Solution:**



Table A-7  $\rightarrow EF = 632 \frac{\text{mg CO}}{\text{kcal}}$  (of heat produced)

• Look up  $\left. \begin{array}{l} \text{for} \\ \text{kerosene} \end{array} \right\} \begin{array}{l} \rho = 804 \text{ kg/m}^3 \\ \text{LHV} = 860 \text{ kcal/mol} \quad (\text{lower heating value}) \\ M = 90 \text{ g/mol} \end{array}$

$$\dot{m}_{\text{CO}} = \left( \frac{632 \text{ mg}}{\text{kcal}} \right) \left( \frac{1 \text{ gal}}{5 \text{ hr}} \right) \left( 860 \frac{\text{kcal}}{\text{mol}} \right) \left( \frac{\text{mol}}{90 \text{ g}} \right) \left( \frac{804 \text{ kg}}{\text{m}^3} \right) \left( \frac{3.785 \times 10^{-3} \text{ m}^3}{\text{gal}} \right) \left( \frac{\text{g}}{10^6 \mu\text{g}} \right) \left( \frac{1000 \mu\text{g}}{\text{kg}} \right)$$

$\uparrow$  EF       $\uparrow$  burn rate       $\uparrow$  LHV       $\uparrow$  1/M       $\uparrow$   $\rho$

$$\dot{m}_{\text{CO}} = 3.7 \text{ g/hr}$$

$\rightarrow$  Answer  $\dot{m}_{\text{CO}} = 4 \frac{\text{g}}{\text{hr}}$

eg. Paint  $\rightarrow$  typical oil-based paint use a VOC  
(volatile organic compound)  
typically a hydrocarbon (HC) like toluene

typical paint contains  $\left. \begin{array}{l} 56\% \text{ solvent} \\ 44\% \text{ pigment \& other stuff} \end{array} \right\} \text{ by mass}$

When you paint, all of solvent eventually goes into the air

Eg. if I use 1 Mg of paint

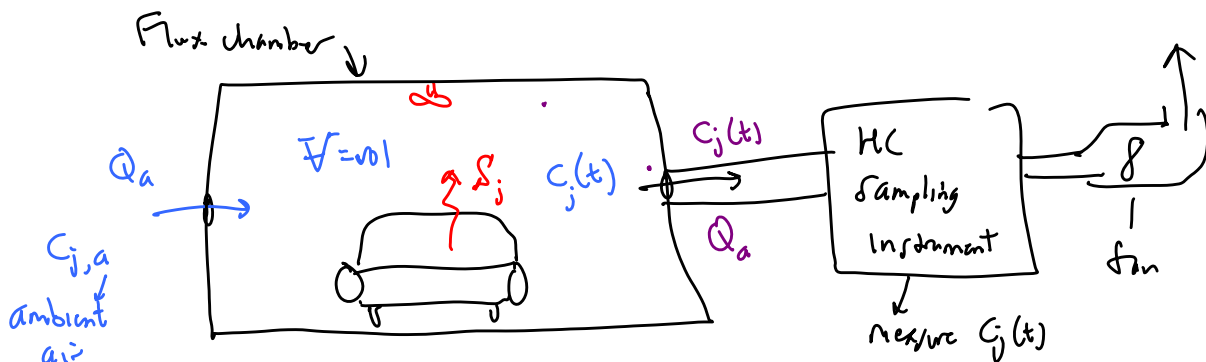
then  $\approx 0.56 \text{ Mg}$  (56%) or 560 kg of solvent

$$\therefore EF = 560 \frac{\text{kg of vapors of HC}}{\text{Mg of paint}}$$

Look at Table A.3  $\rightarrow EF_{\text{paint}} = 560 \frac{\text{kg}}{\text{Mg}}$  ✓

Sec. 4.1.2  $\rightarrow$  Flux chamber  $\equiv$  a clever way to measure emission rates

- Eg.
- A new couch (simulates leather)
  - HCs are released — concern is raised
  - Build a flux chamber to measure  $\dot{m}_{\text{HC}} = S$



Assume the air inside the flux chamber is well mixed

Mass balance for species  $j$  (the HC)

$$\frac{dm_j}{dt} = \dot{m}_{j,\text{in}} + S_j - \dot{m}_{j,\text{out}}$$

↙ [use  $\dot{m}_j = C_j Q$ ]

$$V \frac{dC_j}{dt} = C_{j,a} Q_a + S_j - C_j Q_a \quad (1)$$

1<sup>st</sup>-order ODE

Write (1) in standard form

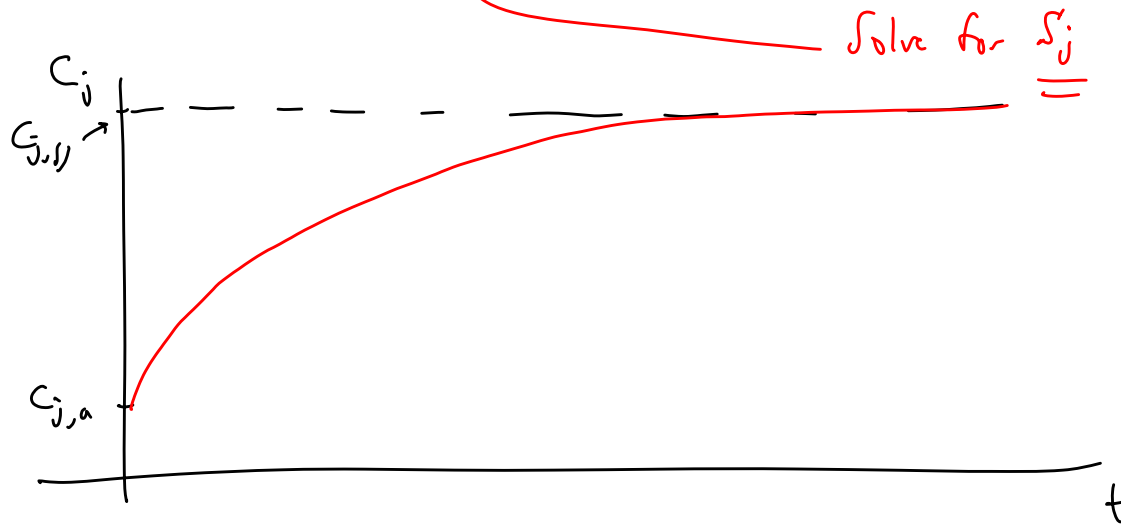
$$\frac{dy}{dt} = B - Ay$$

(1) becomes

$$\frac{dc_j}{dt} = \frac{S_j + Q_a C_{j,a}}{V} - \frac{Q_a}{V} C_j \quad (2)$$

So, if  $S_j, Q_a, C_{j,a}, \text{ and } V = \text{const}$ , we know the analytical solution,

$$C_{j,ss} = \frac{B}{A} = \frac{S_j + Q_a C_{j,a}}{Q_a} = \text{steady-state mol concentration}$$



PROCEDURE:

- measure  $C_{j,a}$  (ambient air mol concentration)
- Measure  $C_j$  until it levels off  $\rightarrow C_j = C_{j,ss}$
- Then solve for  $S_j$ , i.e.

$$S_j = Q_a (C_{j,ss} - C_{j,a})$$

= Source strength =  $\dot{m}_j$  of HC species  $j$  emitted from the coach.

Note: We assume that  $S_j = \text{constant}$ . In reality,  $S_j$  will decay with time, but this takes weeks or months, whereas our experiment takes minutes.