

Design a disk brake to provide maximum torque with sintered metal friction material

given constraints $r_o = 150 \text{ mm}$ $\theta = 35 \text{ deg}$

choose $N = 2$ brake with floating caliper

choose $p_{\text{MAX}} = 2000 \text{ kPa} = 2 \text{ MPa}$ $\mu_{\text{MAX}} = 0.45$ Table 17-1 Norton sintered metal

recommend $r_i = 0.577 r_o = 86.55 \text{ mm}$ Eq. 17.7 Norton

choose $r_i = 85 \text{ mm}$

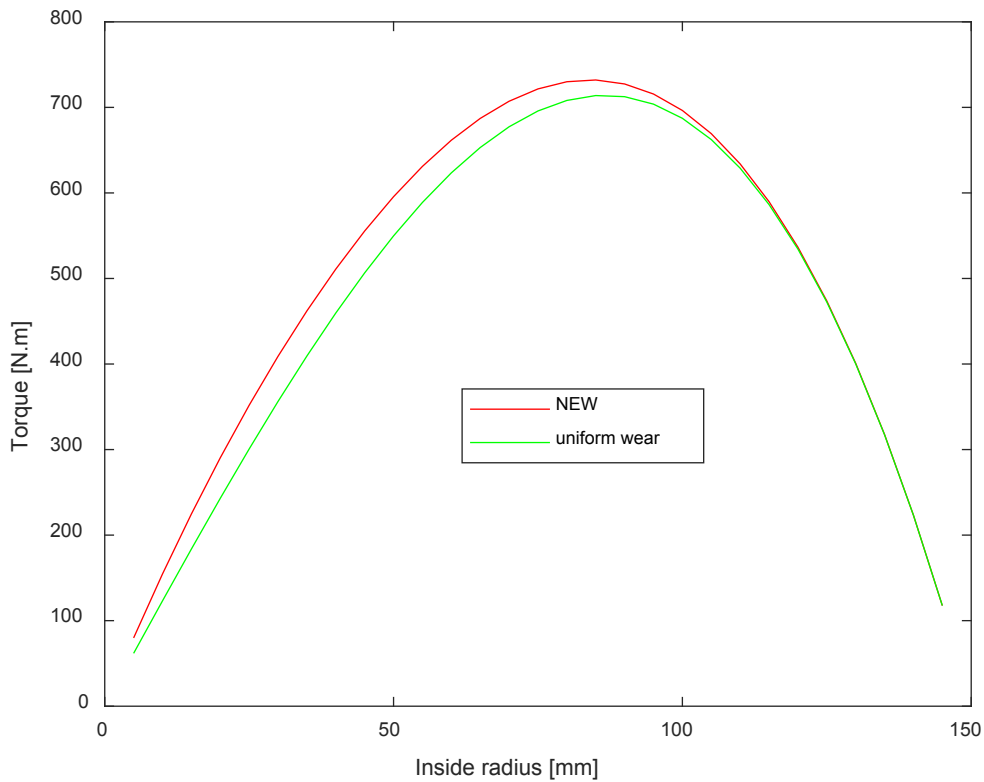
design for long-term use with uniform wear p_{MAX} occurs at r_i Eq. 17.4e

$$F_{\text{MAX}} = r_i \theta p_{\text{MAX}} (r_o - r_i) = (85 \text{ mm})(35 \text{ deg}) \left(\frac{\pi \text{ rad}}{180 \text{ deg}} \right) (2 \text{ MPa})(150 \text{ mm} - 85 \text{ mm}) \quad \text{Eq. 17.5b Norton}$$

$$F_{\text{MAX}} = 6750 \text{ N} = 1518 \text{ lbf}$$

$$T = N \mu F (r_o + r_i) / 2 = 713813 \text{ N.mm} = 713.8 \text{ N.m} = 526.5 \text{ ft.lbf} \quad \text{Eq. 17.6 Norton}$$

r_i [mm]	F_{MAX} [N]	T [N.m]
50	6109	549.8
80	6842	708.1
85	6750	713.8
90	6597	712.5



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% brake.m - disk brake for ME 360
% HJSIII, 18.12.05

% constants
d2r = pi / 180;

% design parameters
N = 2;           % number of rubbing faces
ro = 150;        % outside radius [mm]
theta_deg = 35; % shoe angle [deg]
theta_rad = theta_deg * d2r;
mu = 0.45;       % coefficient of friction - Table 17-1
p_max = 2;       % maximum pressure [MPa] - Table 17-1

% try different inside radii
ri = ( 5 : 5 : 145 ); % inside radius [mm]

% maximum force based on p_max for uniform wear
F = ri * theta_rad .* p_max .* (ro - ri); % [N]

% uniform wear
Tuni = N * mu .* F .* (ro + ri) / 2; % [N.mm]
Tuni = Tuni / 1000; % [N.m]

% new - constant pressure
Tnew = N * mu * F * 2 .* (ro.^3 - ri.^3) / 3 ./ (ro.^2 - ri.^2); % [N.mm]
Tnew = Tnew / 1000; % [N.m]

plot( ri, Tnew, 'r', ri, Tuni, 'g' )
xlabel( 'Inside radius [mm]' )
ylabel( 'Torque [N.m]' )
legend( 'NEW', 'uniform wear' )

% bottom of brake

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NEW - uniform pressure

$$r_i = 85 \text{ mm} \quad F = 6750 \text{ N}$$

$$T_{\text{NEW}} = N \mu F \frac{2 (r_o^3 - r_i^3)}{3 (r_o^2 - r_i^2)} = 732.0 \text{ N.m} = 539.9 \text{ ft.lbf} \quad \text{Eq. 17.3 Norton}$$

$$A = \frac{\theta}{2} (r_o^2 - r_i^2) = \frac{(35 \text{ deg})}{2} \left(\frac{\pi \text{ rad}}{180 \text{ deg}} \right) \left((150 \text{ mm})^2 - (85 \text{ mm})^2 \right) = 4665 \text{ mm}^2 \quad \text{Eq. 17.1b Norton}$$

$$p = F / A = 1.446 \text{ MPa} = 1446 \text{ kPa} \quad \text{OK} \quad \text{Table 17-1 Norton}$$

clutch $N_{\text{FACE}} = 1$ $\theta = 2\pi$ rad = 360 deg woven friction material $\mu = 0.4$

OD = 12 inch ID = 6 inch $F = 700$ lbf

$r_o = 6$ in $r_i = 3$ in

design for long-term use with uniform wear p_{MAX} occurs at r_i

$$T = N \mu F (r_o + r_i) / 2 = 1260 \text{ in.lbf} = 105 \text{ ft.lbf} \quad \text{Eq. 17.6 Norton}$$

$$p_{\text{MAX}} = \frac{F}{r_i \theta (r_o - r_i)} = \frac{700 \text{ lbf}}{(3 \text{ in})(2\pi \text{ rad})(6 \text{ in} - 3 \text{ in})} = 12.4 \text{ psi} \quad \text{Eq. 17.5a Norton}$$

OK Table 17-1 Norton

$$T_{\text{NEW}} = N \mu F \frac{2 (r_o^3 - r_i^3)}{3 (r_o^2 - r_i^2)} = 1307 \text{ in.lbf} = 108.9 \text{ ft.lbf} \quad \text{Eq. 17.3 Norton}$$

recommend $r_i = 0.577 r_o = 3.46$ inch Eq. 17.7 Norton

choose $r_i = 3.5$ inch ID = 7 inch

$$T = 1330 \text{ in.lbf} = 110.8 \text{ ft.lbf} \quad \text{Eq. 17.6 Norton}$$

$$p_{\text{MAX}} = 12.7 \text{ psi} \quad \text{Eq. 17.5a Norton}$$

$$T_{\text{NEW}} = 1361 \text{ in.lbf} = 113.4 \text{ ft.lbf} \quad \text{Eq. 17.3 Norton}$$