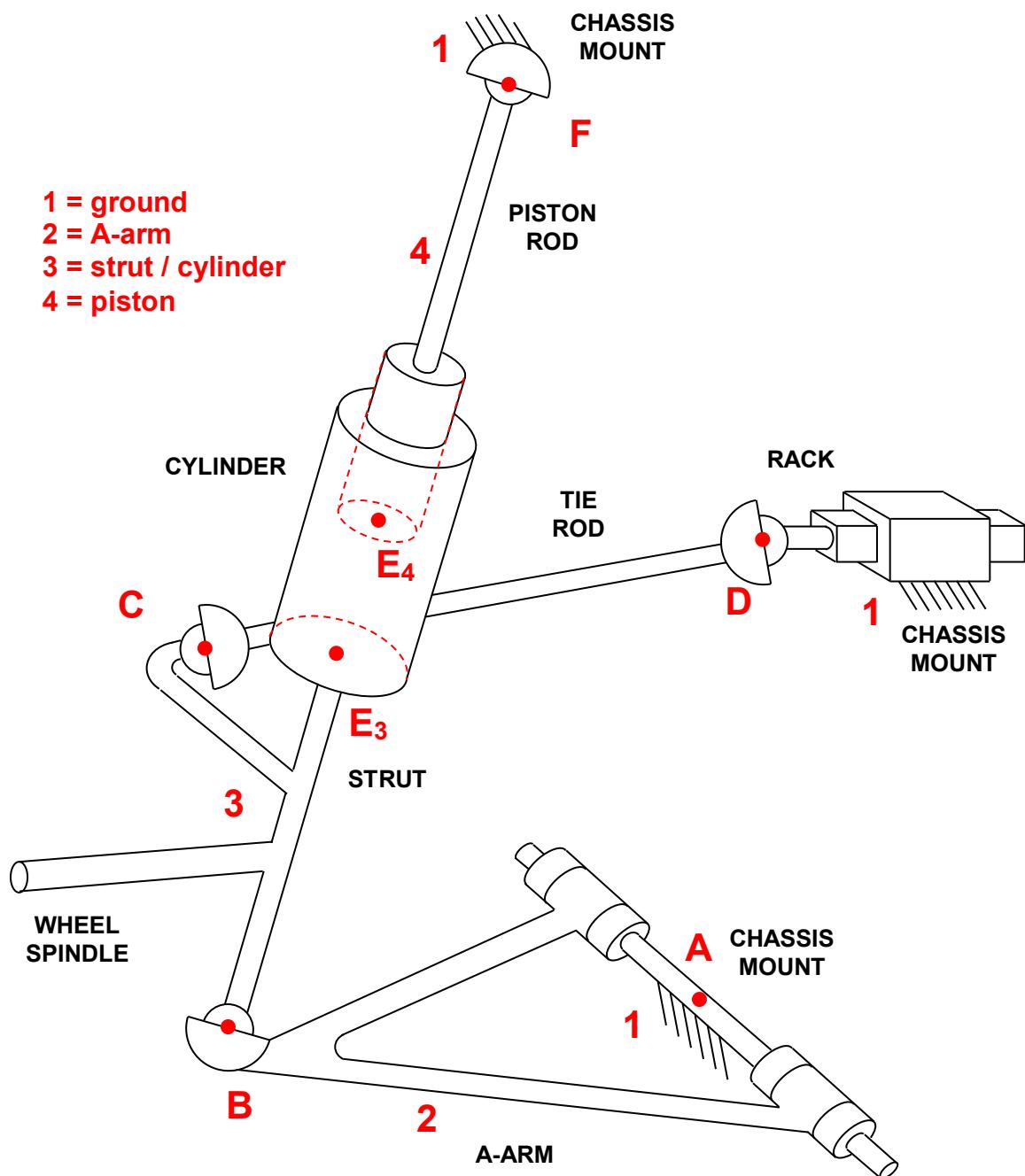


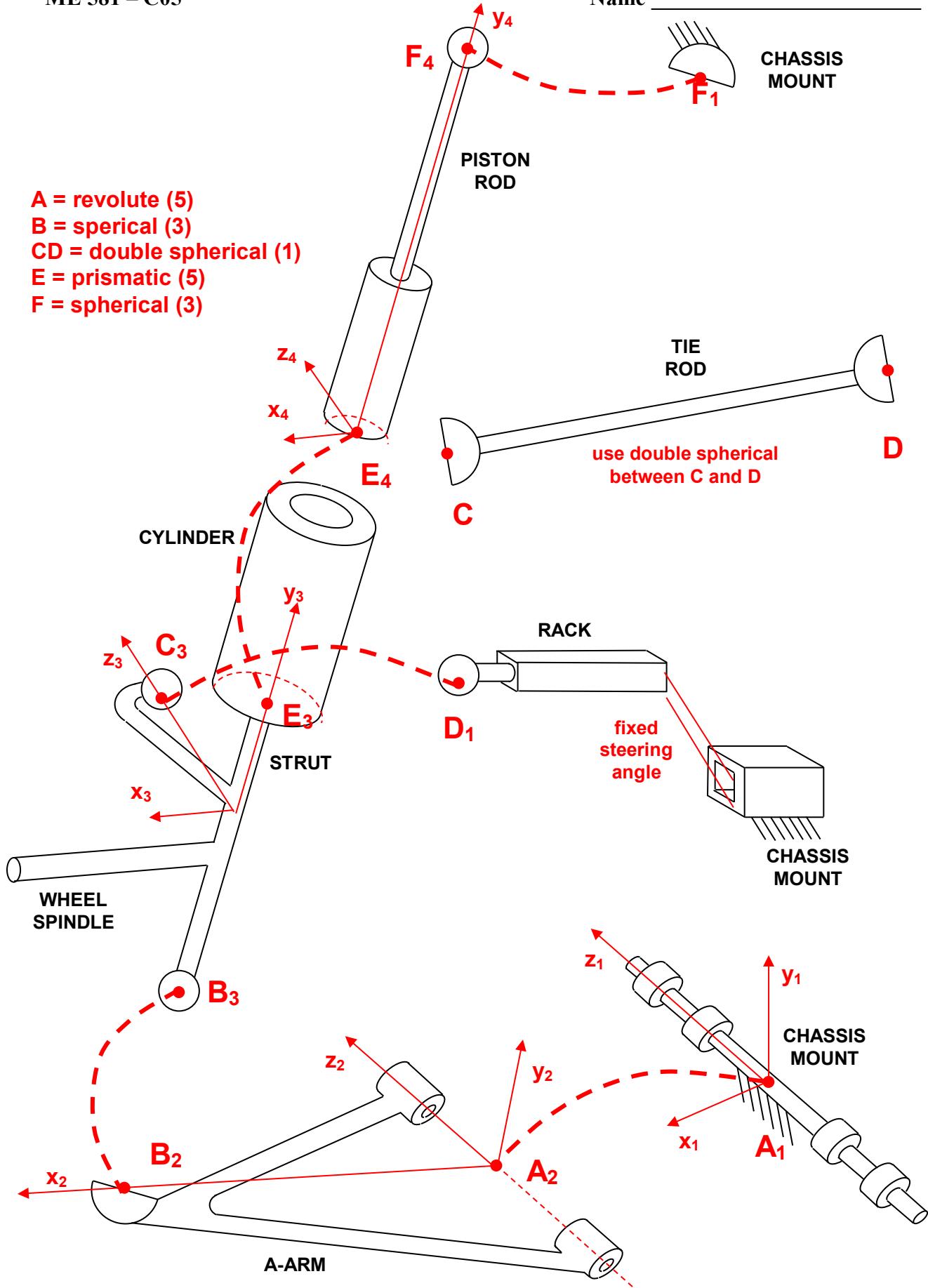
- 1) For a right McPherson strut, attach local coordinate frames to each link for a fixed position of the steering rack. Clearly label all auxiliary points and vectors needed to form constraints.
- 2) Write a corresponding set of generalized coordinates $\{q\}$.
- 3) Symbolically write a constraint vector $\{\Phi\}$ for this mechanism using the vertical absolute translation driver for the strut-spindle assembly $y_3 - y_{3_START} - y_{3_VEL} t = 0$ for $y_{3_VEL} = 4 \text{ cm/sec}$.
- 4) Numerically check the residuals of $\{\Phi\}$ using measurements from model hardware.
- 5) Symbolically write the corresponding Jacobian matrix $[\Phi_q]$.
- 6) Numerically evaluate the elements of the Jacobian and compute the determinant.
- 7) Program your constraints and Jacobian into a Newton-Raphson iterative algorithm to solve position kinematics at any desired time.
- 8) Symbolically write the velocity right-hand-side vector and program to solve for generalized coordinate velocities at any desired time.
- 9) Place your position and velocity algorithms within an outer loop to drive the strut-spindle assembly over $0 \leq t \leq 1 \text{ sec}$. Plot toe-in angle versus vertical position of the strut-spindle assembly. Additionally plot all three components of global angular velocity of the strut-spindle assembly versus time.

EXTRA CREDIT

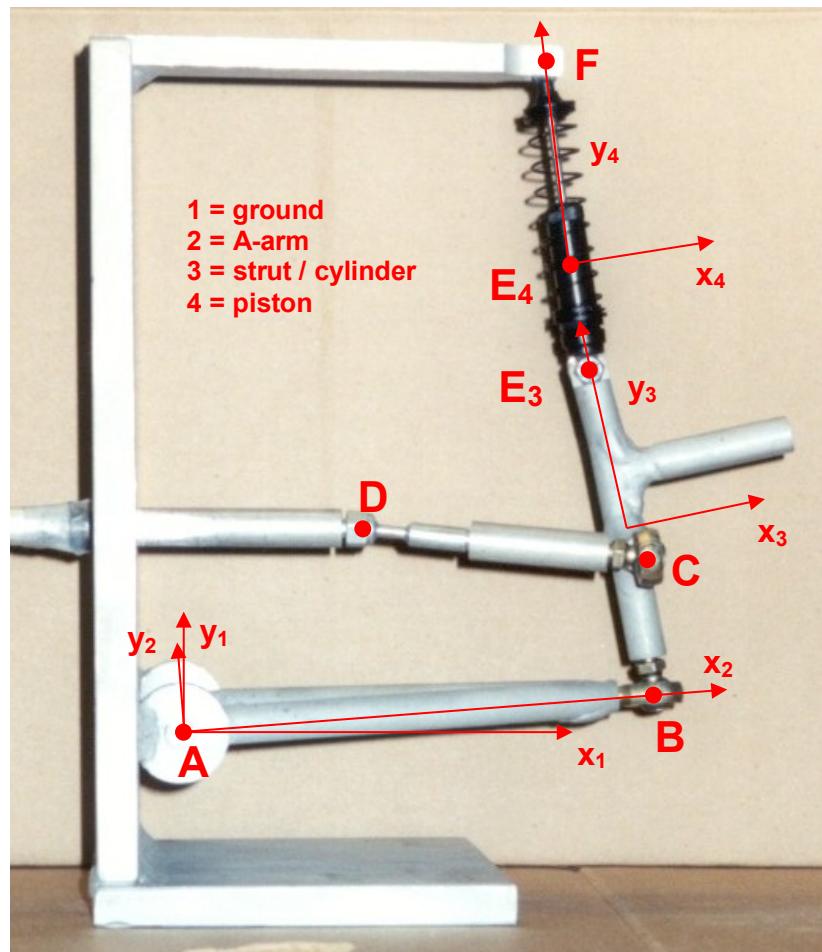
Symbolically write the acceleration right-hand-side vector and program to solve for generalized coordinate accelerations. Plot all three components of global angular acceleration of the strut-spindle assembly versus time.



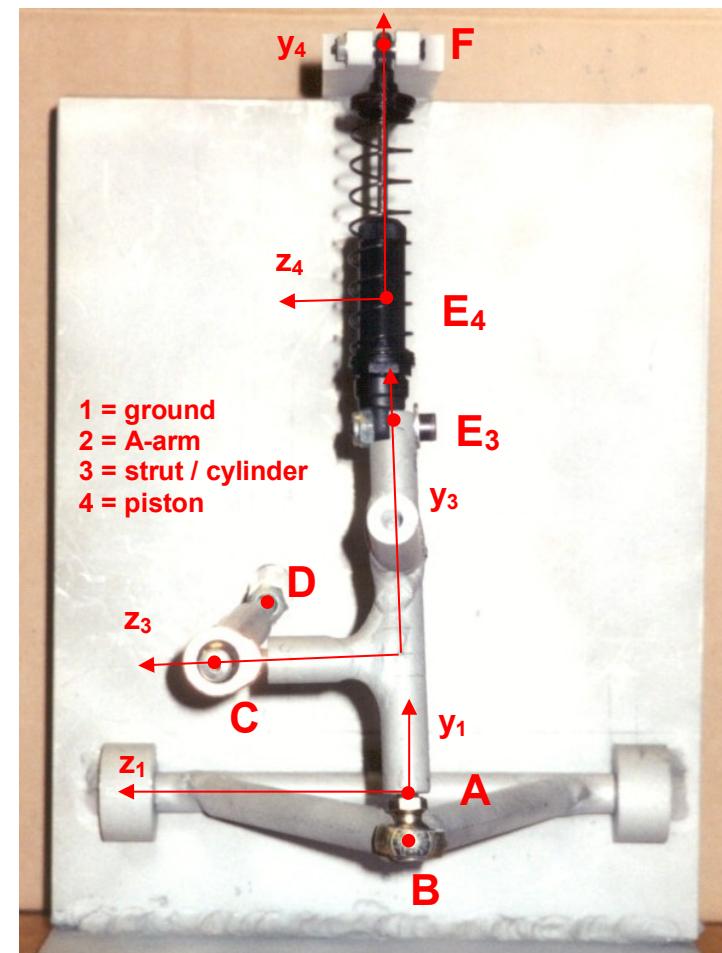
1 = ground
2 = A-arm
3 = strut / cylinder
4 = piston

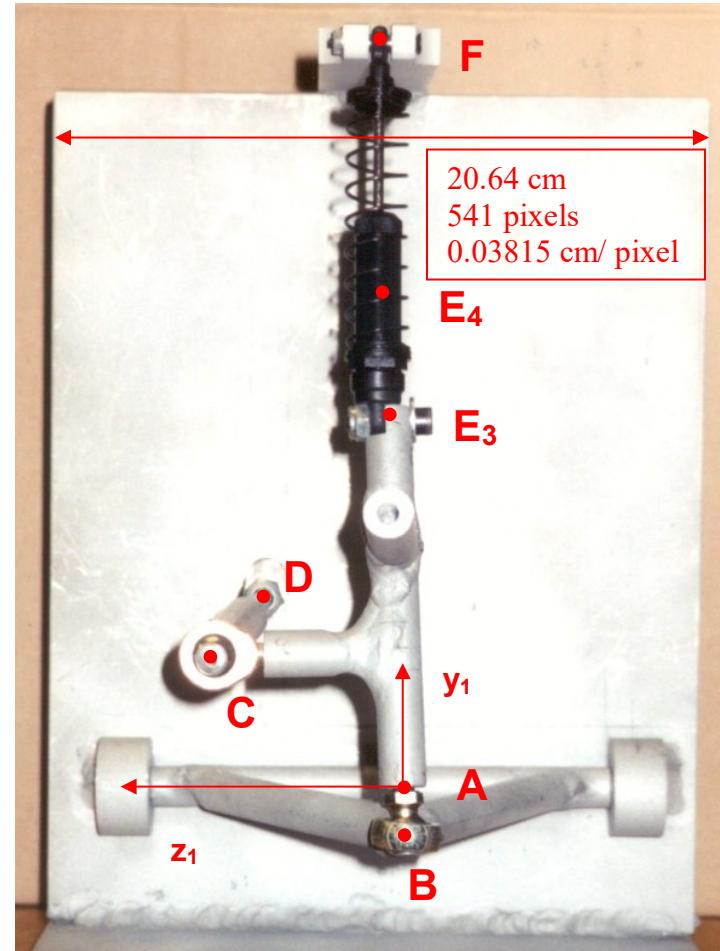
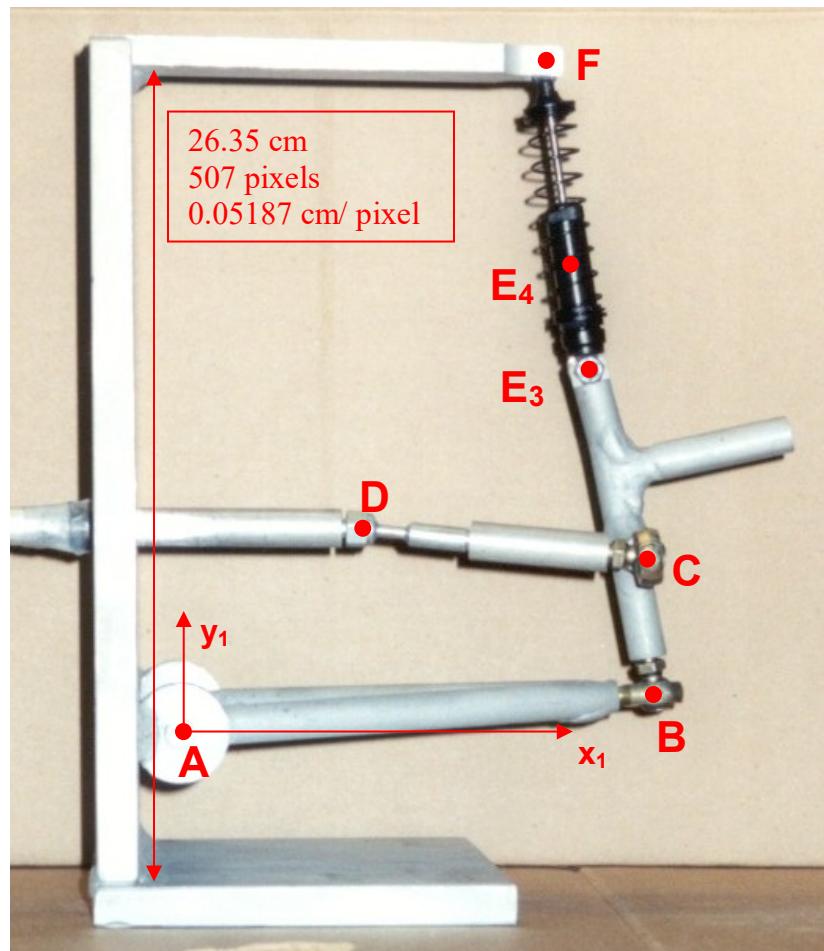


McPherson strut model - rear view



McPherson strut model - side view





scaled from photographs on class web page

cm	x1	y1	z1
A	0	0	0
B	15.70	1.40	0
C	15.49	5.87	5.77
D	6.03	6.81	4.60
E ₃	13.51	12.16	0
E ₄	13.03	15.56	0
F	12.06	22.35	0

Constraints

$$\begin{array}{l}
 \left\{ \begin{array}{l} \{r_1\}^A - \{r_2\}^A \\ \{\hat{f}_2\}^T \{\hat{h}_1\} \\ \{\hat{g}_2\}^T \{\hat{h}_1\} \end{array} \right\} \quad \text{revolute A} \quad \begin{array}{l} \text{revA}, i = 2, j = 1 \\ f_2 h_1, i = 2, j = 1 \\ g_2 h_1, i = 2, j = 1 \end{array} \\
 \\
 \{r_2\}^B - \{r_3\}^B \quad \text{spherical B} \quad \text{sphB}, i = 3, j = 2 \\
 \\
 \{d_{ij}\}^T \{d_{ij}\} - CD^2 \quad \{d_{ij}\} = \{r_i\}^D - \{r_3\}^C \quad 1D - 3C, i = 3, j = 1 \\
 \\
 \left\{ \begin{array}{l} \{r_2\} \\ \{p_2\} \\ \{r_3\} \\ \{p_3\} \\ \{r_4\} \\ \{p_4\} \end{array} \right\}_{21x1} \quad \left\{ \begin{array}{l} \{\hat{f}_3\}^T \{\hat{g}_4\} \\ \{\hat{h}_3\}^T \{\hat{g}_4\} \\ \{\hat{f}_3\}^T \{d_{ij}\} \\ \{\hat{h}_3\}^T \{d_{ij}\} \\ \{\hat{f}_3\}^T \{\hat{h}_4\} \end{array} \right\}_{21x1} \quad \begin{array}{ll} & f_3 g_4, i = 3, j = 4 \\ & h_3 g_4, i = 3, j = 4 \\ \text{prismatic E} & \{d_{ij}\} = \{r_4\}^E - \{r_3\}^E \quad f_3, i = 3, j = 4 \\ & h_3, i = 3, j = 4 \\ & f_3 h_4, i = 3, j = 4 \end{array} \\
 \\
 \{r_i\}^F - \{r_4\}^F \quad \text{spherical F} \quad \text{sphF}, i = 4, j = 1 \\
 \\
 \{p_2\}^T \{p_2\} - 1 \quad \text{Euler parameters} \quad p2 \\
 \{p_3\}^T \{p_3\} - 1 \quad & p3 \\
 \{p_4\}^T \{p_4\} - 1 \quad & p4 \\
 \\
 y_3 - y_{3_START} - y_{3_VEL} t \quad \text{driver} \quad \text{driver}
 \end{array}$$

Velocity

$$\left\{ v \right\}_{21x1} = \begin{pmatrix} 0_{20x1} \\ y_{3_VEL} \end{pmatrix}$$